

Derivate

$$\partial(c) = 0$$

$$\partial(f(x)) = 1$$

$$\partial(f(x) \pm g(x)) = f'(x) \pm g'(x)$$

$$\partial(f(x)g(x)) = f'(x)g(x) + f(x)g'(x)$$

$$\partial\left(\frac{f(x)}{g(x)}\right) = \frac{f'(x)g(x) - f(x)g'(x)}{g^2(x)} \quad \forall g(x) \neq 0$$

$$\partial(\sqrt{f(x)}) = \frac{f'(x)}{2\sqrt{f(x)}}$$

$$\partial(f^{-1}(y)) = \frac{1}{f'[f^{-1}(y)]}$$

$$\partial\left(\frac{1}{f(x)}\right) = \partial(f^{-1}(x)) = -\frac{f'(x)}{[f(x)]^2}$$

$$\partial(\ln(x)) = \frac{1}{x} \quad \forall x > 0$$

$$\partial(\ln|f(x)|) = \frac{f'(x)}{f(x)} \quad \forall f(x) \neq 0$$

$$\partial([\ln(x)]^x) = \frac{[\ln(x)]^x}{\ln(x) + \ln(\ln(x))}$$

$$\partial(\log_a(x)) = \frac{1}{x} \log_a(e) = \frac{1}{x \cdot \ln(a)} \quad \forall \begin{cases} a > 0 \\ a \neq 1 \\ x > 0 \end{cases}$$

$$\partial(e^{cx}) = ce^{cx}$$

$$\partial(e^{f(x)}) = e^{f(x)} \cdot f'(x)$$

$$\partial(f[g(x)]) = f'[g(x)] \cdot g'(x)$$

$$\partial(f(x)^n) = n \cdot [f(x)]^{n-1} \cdot g'(x) \quad \forall n \in \mathbb{N}$$

$$\partial(f(x)^{g(x)}) = \partial(e^{g(x)\ln[f(x)]}) = f(x)^{g(x)} [g'(x) \cdot \ln(f(x)) + \frac{g(x)f'(x)}{f(x)}] \quad \forall f(x) > 0$$

$$\partial\left(e^{\frac{1}{\ln(x)}}\right) = -\frac{e^{\frac{1}{\ln(x)}}}{x \ln^2(x)}$$

$$\partial(a^x) = a^x \cdot \ln(a) \quad \forall a > 0$$

$$\partial(a^{f(x)}) = a^{f(x)} \cdot \ln(a) \cdot f'(x) \quad \forall a > 0$$

$$\partial(x^n) = nx^{n-1} \quad \forall \begin{cases} x > 0 \\ n \in \mathbb{N} \end{cases}$$

$$\partial(x^x) = x^x [1 + \ln(x)]$$

$$\partial\left(\frac{1}{x^n}\right) = -\frac{n}{x^{n+1}}$$

$$\partial(\sqrt{x}) = \frac{1}{2\sqrt{x}}$$

$$\partial(\sqrt[n]{x}) = \frac{1}{n\sqrt[n]{x^{n-1}}} \quad : \mathbb{R}_+ \rightarrow \mathbb{R}_+$$

$$\partial(\sqrt[n]{x}) = [1 - \ln(x)] \cdot x^{\left(\frac{1}{n}\right)-1}$$

$$\partial(|x|) = \frac{x}{|x|} = \frac{|x|}{x} \quad \forall x \neq 0$$

$$\partial(|f(x)|) = \frac{f(x)}{|f(x)|} f'(x) = \frac{|f(x)|}{f(x)} f'(x)$$

$$\partial(\sin(x)) = \cos(x)$$

$$\partial(\sin^2(x)) = 2 \cdot \sin(x) \cdot \cos(x)$$

$$\partial\left(\frac{1}{\sin(x)}\right) = -\frac{\cos(x)}{\sin^2(x)}$$

$$\partial(\cos(x)) = -\sin(x)$$

$$\partial(\cos^2(x)) = -2 \cdot \sin(x) \cdot \cos(x)$$

$$\partial\left(\frac{1}{\cos(x)}\right) = \frac{\sin(x)}{\cos^2(x)}$$

$$\partial(\sin(x)^{\cos(x)}) = \sin(x)^{\cos(x)} \cdot \left[\frac{\cos^2(x)}{\sin(x) - \sin(x) \cdot \ln(\sin(x))} \right]$$

$$\partial(\cos(x)^{\sin(x)}) = \cos(x)^{\sin(x)} \cdot [\cos(x) \cdot \ln(\cos(x)) - \sin(x) \cdot \tan(x)]$$

$$\partial(\tan(x)) = \frac{1}{\cos^2(x)} = 1 + \tan^2(x) \quad \forall x \in \mathbb{R} - \left\{ \frac{\pi}{2} + k\pi \right\}$$

$$\partial(\tan^2(x)) = \frac{2\tan(x)}{\cos^2(x)}$$

$$\partial(\cot(x)) = -\frac{1}{\sin^2(x)} = -[1 + \cot^2(x)]$$

$$\partial(\arcsin(x)) = \frac{1}{\sqrt{1-x^2}} \quad :]-1, 1[\rightarrow \left[-\frac{\pi}{2}, \frac{\pi}{2} \right]$$

$$\partial(\arccos(x)) = -\frac{1}{\sqrt{1-x^2}} \quad :]-1, 1[\rightarrow]0, \pi[$$

$$\partial(\arctan(x)) = \frac{1}{1+x^2} \quad : \mathbb{R} \rightarrow \left] -\frac{\pi}{2}, \frac{\pi}{2} \right[$$

$$\partial(ArcCtg(x)) = -\frac{1}{1+x^2} : \mathbb{R} \rightarrow]0, \pi[$$

$$\partial(SinH(x)) = CosH(x) : \mathbb{R} \rightarrow \mathbb{R}$$

$$\partial(CosH(x)) = SinH(x) : \mathbb{R} \rightarrow \mathbb{R}$$

$$\partial(TgH(x)) = \frac{1}{CosH^2(x)} = 1 + TgH^2(x)$$

$$\partial(CtgH(x)) = -\frac{1}{SinH^2(x)} = 1 - CtgH^2(x)$$

$$\partial(SettSinH(x)) = \frac{1}{\sqrt{1+x^2}}$$

$$\partial(SettCosH(x)) = \frac{1}{\sqrt{x^2-1}}$$

$$\partial(SettTgH(x)) = \frac{1}{1-x^2}$$

$$\partial(SettCtgH(x)) = \frac{1}{1-x^2}$$