

Limiti

$$\lim_{x \rightarrow 0} \frac{\sin(ax^k)}{bx^k} = \frac{a}{b}$$

$$\lim_{x \rightarrow 0} \frac{\cos(ax^k)}{bx^k} = \frac{a}{b}$$

$$\lim_{x \rightarrow 0} \frac{\operatorname{Tg}(ax^k)}{bx^k} = \frac{a}{b}$$

$$\lim_{x \rightarrow 0} \frac{1 - \cos(x)}{x} = 0$$

$$\lim_{x \rightarrow 0} \frac{1 - \cos(x)}{x^2} = \frac{1}{2}$$

$$\lim_{x \rightarrow 0} \sqrt[x]{1+x} = e$$

$$\lim_{x \rightarrow 0} \left(1 + \frac{\alpha}{x}\right)^{\beta x} = e^{\alpha\beta}$$

$$\lim_{x \rightarrow 0} \left(1 - \frac{1}{x}\right)^x = \frac{1}{e}$$

$$\lim_{x \rightarrow 0} \frac{\log_b(1+x)}{x} = \frac{1}{\ln(b)}$$

$$\lim_{x \rightarrow 0} \frac{a^{mx} - 1}{x} = \ln(a^m) = m \ln(a)$$

$$\lim_{x \rightarrow 0} \frac{(1+x)^\alpha - 1}{\beta x} = \frac{\alpha}{\beta}$$

$$\lim_{x \rightarrow 0^+} x^\alpha \ln(x) = 0$$

$$\lim_{x \rightarrow +\infty} \frac{\ln(x)}{x^\alpha} = 0$$

$$\lim_{x \rightarrow +\infty} [x - \alpha \ln(x)] = +\infty$$

$$\lim_{x \rightarrow +\infty} \frac{e^x}{x^\alpha} = +\infty \quad \forall \alpha > 0$$

$$\lim_{x \rightarrow +\infty} \left(\frac{x^\alpha}{\beta^x}\right) = 0 \quad \forall \alpha > 0 \text{ e } \beta > 1$$

$$\lim_{x \rightarrow +\infty} \frac{\ln(x)}{\alpha^x} = 0 \quad \forall \alpha > 1$$

$$\lim_{x \rightarrow \pm\infty} \left(1 + \frac{\alpha}{x}\right)^x = e^\alpha$$

$$\lim_{x \rightarrow \pm\infty} x \ln\left(1 + \frac{1}{x}\right) = 1$$

$$\lim_{x \rightarrow x_0} f(x)^{g(x)} = e^{\lim_{x \rightarrow x_0} [(f(x)-1)g(x)]}$$

$$\lim_{n \rightarrow +\infty} (1 + a_n)^{\frac{1}{a_n}} = e$$

$$\lim_{n \rightarrow +\infty} \left(1 + \frac{1}{a_n}\right)^{a_n} = e$$

$$\lim_{n \rightarrow \infty} \frac{\sin(a_n)}{a_n} = \lim_{n \rightarrow \infty} \frac{\operatorname{Tg}(a_n)}{a_n} = 1$$

$$\lim_{n \rightarrow +\infty} \frac{a_n^{a_n} - 1}{a_n} = \log(a)$$

$$\lim_{n \rightarrow +\infty} \frac{(1 + a_n)^\alpha - 1}{a_n} = \alpha$$

$$\lim_{n \rightarrow \infty} \frac{\ln(n)}{n} = 0$$

$$\lim_{x \rightarrow 0} \sin(x) = 0$$

$$\lim_{x \rightarrow 0} \cos(x) = 1$$

$$\lim_{x \rightarrow 0} \frac{\sin(kx)}{x} = k$$

$$\lim_{x \rightarrow 0} \sqrt{\frac{\sin(x)}{x}} = 1$$

$$\lim_{x \rightarrow +\infty} [x + \sin(x)] = +\infty$$

$$\lim_{x \rightarrow 0} \frac{\operatorname{Tg}(x)}{x} = 1$$

$$\lim_{x \rightarrow 0} \frac{1 - \cos(2x)}{x^2} = 2$$

$$\lim_{x \rightarrow \infty} x \cdot \sin\left(\frac{1}{x}\right) = 1$$

$$\lim_{x \rightarrow 0} x \cdot \sin\left(\frac{1}{x}\right) = 0$$

$$\lim_{x \rightarrow 0} \left(\frac{1}{x^2}\right) = +\infty$$

$$\lim_{x \rightarrow 0} \left(\frac{1}{x}\right) = \infty$$

$$\lim_{x \rightarrow 0} \frac{e^x - 1}{x} = 1$$

$$\lim_{x \rightarrow 1} \frac{\ln(x)}{x-1} = 1$$

$$\lim_{x \rightarrow +\infty} \frac{x^k}{p \cdot [\ln(x)]} = +\infty \quad \forall k, p > 0$$

$$\lim_{x \rightarrow 0} \frac{a^x - b^x}{x} = \ln\left(\frac{a}{b}\right)$$

$$\lim_{x \rightarrow 0} \left[\frac{\sin(x)}{x}\right]^x = 1$$

$$\begin{aligned}
& \lim_{x \rightarrow +\infty} \sqrt[n]{x} = +\infty & 1^\infty \\
& \left. \begin{aligned} \lim_{x \rightarrow +\infty} a^x &= +\infty \\ \lim_{x \rightarrow -\infty} a^x &= 0 \end{aligned} \right\} \forall a > 1 & \infty^0 \\
& \left. \begin{aligned} \lim_{x \rightarrow +\infty} a^x &= 0 \\ \lim_{x \rightarrow -\infty} a^x &= +\infty \end{aligned} \right\} \forall 0 < a < 1 \\
& \lim_{x \rightarrow +\infty} x^a = \begin{cases} +\infty & \forall b > 0 \\ 0 & \forall b < 0 \end{cases} \\
& \left. \begin{aligned} \lim_{x \rightarrow +\infty} \log_a(x) &= +\infty \\ \lim_{x \rightarrow 0^+} \log_a(x) &= -\infty \end{aligned} \right\} \forall a > 1 \\
& \left. \begin{aligned} \lim_{x \rightarrow +\infty} \log_a(x) &= -\infty \\ \lim_{x \rightarrow 0^+} \log_a(x) &= +\infty \end{aligned} \right\} \forall 0 < a < 1 \\
& \lim_{x \rightarrow \infty} \frac{[\log_a(x)]^\alpha}{x} = 0 \\
& \lim_{x \rightarrow +\infty} \frac{[\log_a(x)]^\beta}{x^\alpha} = 0 \quad \forall \alpha > 0, \forall \beta \\
& \lim_{x \rightarrow \infty} (1+x)^{\frac{1}{x}} = e \\
& \lim_{x \rightarrow 0} \frac{\ln(1+x)}{x} = 1 \\
& \lim_{x \rightarrow +\infty} \ln(x) = +\infty \\
& \lim_{x \rightarrow 0^+} \ln(x) = -\infty \\
& \lim_{x \rightarrow x_0} \left[1 + \frac{1}{f(x)} \right]^{f(x)} = e \\
& \lim_{x \rightarrow x_0} [1 + f(x)]^{\frac{1}{f(x)}} = e \\
& \lim_{x \rightarrow 0} [\cos(x)]^{\frac{1}{x^2}} = \frac{1}{\sqrt{e}} \\
& \lim_{x \rightarrow +\infty} \operatorname{ArcTg}[\ln(x)] = \frac{\pi}{2} \\
& \lim_{x \rightarrow 0} \ln \left| x \cdot \sin \left(\frac{1}{x} \right) \right| = -\infty
\end{aligned}$$

Forme indeterminate

$$+\infty - \infty$$

$$-\infty + \infty$$

$$0 \cdot (\pm\infty)$$

$$\frac{0}{0}$$

$$\frac{\infty}{\infty}$$

$$\frac{\infty}{\infty}$$

$$0^0$$